

## AP Statistics – Inference with Two Sample Means

**THE NOT-ENOUGH SHOES PROBLEM** How many pairs of shoes do teenagers have? To find out, a group of AP Statistics students conducted a survey in which they selected two separate random samples of 12 male students and 12 female students from their school. Then they recorded the number of pairs of shoes that each respondent reported having. The data is displayed below.

### Females:

12	13	15	15	19	21	22	24	26	31	34	41
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Mean: 22.75                      Standard Deviation: 8.9861                      Number of students: 12

### Males

4	5	5	6	7	8	10	10	11	12	14	17
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Mean: 9.0833                      Standard Deviation: 3.988                      Number of students: 12

a) Construct and interpret a 95% confidence interval for the difference in the mean number of pairs of shoes owned between male and female students at this high school.

### 2-sample t-interval

*(use calculator!)*

**(7.6176, 19.7157)**

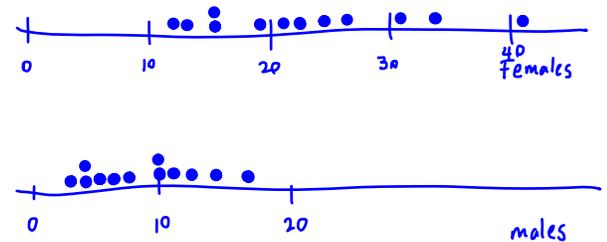
**df = 15.171**

We are 95% confident that the true difference in the **mean** number of shoes owned between male and female students (female – male) at this high school is between 7.62 and 19.72 pairs of shoes.

Conditions for inference:

- **Independent Random Samples:**  
The data was collected via separate (thus, reasonably independent) random samples of male and female students.
- **Nearly Normal Condition:**  
The plots show some slight skewness, but with no major outliers, normality should be plausible for both groups.

Pairs of shoes:



b) Carefully interpret the meaning of the 95% confidence level in context.

If we repeated this method maaaaaaaaaaaaany times, about 95% of the resulting intervals would contain the true difference in the mean number of shoes owned between male and female students at this high school

## AP Statistics – Inference with Two Sample Means

**“EACH DAY I AM GETTING BETTER IN MATH”** A subliminal message is below our threshold of awareness but may nonetheless influence us. Can subliminal messages help students learn math? A group of 18 students who had failed the mathematics part of the City University of New York Skills Assessment Test agreed to participate in a study to find out. All received a daily subliminal message, flashed on a screen too rapidly to be consciously read. The 10 students in group “A” (assigned at random) were exposed to “Each day I am getting better in math.” The control group of 8 students (group “B”) was exposed to a neutral message, “People are walking on the street.” All 18 students participated in the summer program designed to raise their math skills, and all took the assessment test again at the end of the program. The tables below gives data on the each subject’s test score improvement:

### Message “A” (10 students)

6	7	12	11	15	16	11	13	13	10
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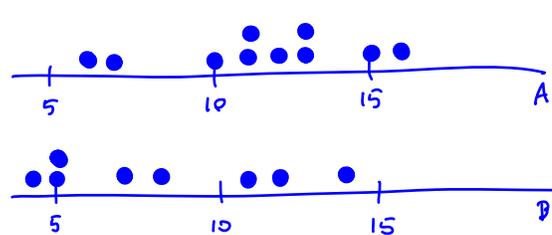
Mean: 11.4      Standard Deviation: 3.17

### Message “B” (8 students)

11	5	4	8	14	5	7	12
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Mean: 8.25      Standard Deviation: 3.69

NYSAT score improvement:



**At the 10% level of significance, do the data provide evidence that the mean NYSAT score improvement for students exposed to message “A” is higher than the mean NYSAT score improvement for students exposed to message “B”?**

### 2-sample t-test

$\mu_1$  = true mean score improvement for students receiving message “A”

$\mu_2$  = true mean score improvement for students receiving message “B”

$$H_0: \mu_1 = \mu_2$$

$$H_A: \mu_1 > \mu_2$$

(use the calculator!)

$$t = 1.91356$$

$$p\text{-value} = 0.0382$$

$$\alpha = 0.10$$

$$df = 13.9187$$

### Conditions:

- Students were randomly assigned to receive one of the two subliminal messages
- Based on graphs of the sample data for both groups, normality is plausible (no major outliers or obvious skew to either graph).

Since  $p < \alpha$ , we reject the  $H_0$ .

We have sufficient evidence that the mean score for students receiving subliminal message “A” is higher than for those receiving message “B”.